

## SYNTAX AND SEMANTICS OF PLURAL

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The analysis of singular and plural has been a rather neglected topic in transformational grammar. Because of the marginal interest in semantic phenomena the number distinction has been handled as a feature like  $\langle \pm \text{human} \rangle$  or gender. Furthermore, it has been assumed that the number-feature is inherent in the noun rather than the noun phrase (Chomsky 1967, Postal 1966, Rosenbaum 1968, Perlmutter 1968 - I can find no later accounts of a different persuasion).

In this paper I want to investigate the number distinction from a semantic point of view. Since Montague's work provides the only framework so far in which an explicit semantic representation can be accomplished, I will present my investigation as an extension of Montague's "Proper Treatment of Quantification" (hence PTQ). PTQ provides a complete treatment of syntax and semantics. This 'vertical completeness' has the consequence that a large number of linguistic phenomena is not incorporated in the 'fragment' - among them the singular/plural distinction.

To incorporate the number distinction on the syntactic as well as the semantic level in PTQ one could postulate singular versus plural nouns. This is the way in which Mike Bennett (1972) has extended PTQ to the plural. Bennett derives plural nouns from singular nouns syntactically, but assumes the corresponding semantic rule to be the identity mapping. Renate Bartsch (1972), on the other hand, even proposes that plural nouns translate into expressions that are of a different semantic type than singular nouns.

In this paper, however, singular and plural will be treated as a feature of the quantifier rather than the noun. This has the syntactic advantage over Bennett's solution that no cooccurrence restrictions are necessary in order to prevent forms like \*every girls. Semantically it has the advantage that a singular noun and a distributive plural noun are translated into expressions of the same type and can thus be handled by the same general rules.

Let us begin with the distinction between distributive plurals versus collective plurals. Sentence

1) All the girls walked  
is an example for a distributive plural, while

2) All the girls gathered  
 is an example for a collective plural. The sentence  
 3) All the boys lifted the piano  
 is ambiguous between a collective and a distributive  
 reading. On the collective reading, all the boys  
 lifted the piano together. Thus it would be false to  
 entail from this reading that 'a<sub>0</sub> lifted the piano',  
 'a<sub>1</sub> lifted the piano', ... etc. where a<sub>0</sub>, a<sub>1</sub> etc.  
 are members of the set of boys in question.<sup>1</sup> On the  
 distributive reading, however, we have to obtain such  
 entailments, since on this reading each boy lifts the  
 piano by himself.

Let us define the translation of a distributive  
plural similar to Montague's singular noun phrases.

For example, a girl translates in PTQ as

4)  $\widehat{PVx}[girl'(x) \wedge P\{x\}]$ .

Now the plural of a girl is girls. For the plural we  
 want to insure that girl' holds at least for two indi-  
 vidual concepts. This is expressed in formula

5)  $PVxVy[\neg(x=y) \wedge girl'(x) \wedge girl'(y) \wedge P\{x\} \wedge P\{y\}]$

Note that (5) is an appropriate translation for a dis-  
 tributive plural since it entails (via simplification)  
 that of each girl the property denoted by P holds. In  
 order to have a more simple notation we abbreviate (5)  
 as

6)  $\widehat{PV}_2[girl'(x) \wedge P\{x\}]$ .

In order to implement collective plurals, how-  
 ever, we have to define a new kind of verbs as well as  
 a new kind of noun phrases. A verb like the intransi-  
 tive gather, for example, does not take subjects that  
 denote single individuals, but only subjects that de-  
 note a group or a set of individuals. Therefore the  
 translation of gather should be a function that maps  
 sets of individual concepts, i.e. arguments of type  
 $\langle\langle s, e \rangle, t \rangle$ , into truthvalues. Thus the verb gather  
 should be semantically of type  $\langle\langle\langle s, e \rangle, t \rangle, t \rangle$ .

However, a function of type  $\langle\langle\langle s, e \rangle, t \rangle, t \rangle$  has no  
 corresponding category in the syntax of PTQ. (This  
 is a point Mike Bennett overlooked in his extension  
 on plural. Otherwise the semantics of the here pre-  
 sented treatment of collective plurals parallel Mike  
 Bennett's approach). The reason that  $\langle\langle\langle s, e \rangle, t \rangle, t \rangle$   
 has no corresponding expression among the syntactic  
 categories lies in the way in which Montague defines  
 the function f that maps the syntactic categories into  
 types of intensional logic. f is defined as follows:

$f(e) = e$

$f(t) = t$

$f(A/B) = f(A//B) = \langle\langle s, f(B) \rangle, f(A) \rangle$  whenever  
 $A, B \in \text{CAT}$ .

Therefore, instead of defining gather' as a function from sets of individual concepts to truth-values, we will define it as a function from properties of individual concepts into truthvalues (the property of individual concepts is the intension of sets of individual concepts!). Thus gather' will range over variables P,Q of type  $\langle s, \langle \langle s, e \rangle, t \rangle \rangle$ . The meaning postulate

7)  $\square [\delta(P) \leftrightarrow \delta_*(\forall P)]$ , where  $\delta$  is an  $\overline{IV}$  (i.e. a verb like gather, collide, be similar etc.)

will lower expressions like gather'(P) from a set of properties of individual concepts to a set of sets of individual concepts. Indeed, we can lower  $\delta(P)$  to  $\delta_*(M)$ , i.e. sets of individuals, since verbs that take collective plural terms as subject (or object) seem to be always extensional. We will therefore adopt the following meaning postulate:

8)  $\square [\delta(P) \leftrightarrow \delta_*(\forall M)]$ , where  $\delta$  is an  $\overline{IV}$ .

We are using here the same technique Montague employed when he postulated a meaning postulate that lowers for example walk'(x) to walk\_\*'(u).

According to our discussion a verb like gather will be of the syntactic category  $t/(t//e)$ , which is abbreviated as  $Cat_{\overline{IV}}$ . The semantic type of expressions of  $Cat_{\overline{IV}}$  is  $\langle \langle s, \langle \langle s, e \rangle, t \rangle \rangle, t \rangle$ . Furthermore, we define the variable R of type  $\langle s, \langle \langle s, \langle \langle s, e \rangle, t \rangle \rangle, t \rangle \rangle$ , which ranges over properties of properties of individual concepts. By means of R we define the translation of the collective pronoun they<sub>n</sub>:

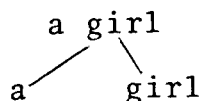
9) collective they<sub>n</sub> translates as  $\widehat{RR}\{P_n\}$ , where  $P_n$  is a variable of type  $\langle s, \langle \langle s, e \rangle, t \rangle \rangle$  defined as  $(\hat{y}[x_n=y])$ .

Collective they<sub>n</sub> is the sole member of the set  $B_{\overline{T}}$ , where  $\overline{T} = t//e^n$ . The derivation of the translation of they<sub>n</sub> gather will run as<sub>n</sub> follows ( - once all the rules are supplied)

$$\begin{aligned} & \widehat{RR}\{P_n\} (\wedge \text{gather}') \\ & \wedge \text{gather}'\{P_n\} \\ & \text{gather}'(\hat{y}[x_n=y]) \\ & \text{gather}'_*(\hat{u}[v_n=u]) \end{aligned}$$

After this discussion of the semantic properties of distributive versus collective plural noun phrases let us turn to the syntactic rules for handling plural. R. Thomason (1972) suggested to derive quantified T-phrases from CN-phrases via a rule of functional appli-

cation (rather than via a basic as in PTQ). According to Thomason, a term like a girl is analyzed as



where a is of category T/CN.  $a(n)$  translates into  $\overline{Q}PVx[Q\{x\} \wedge P\{x\}]$ . Thus a girl translates as

$$PVx[\text{girl}'(x) \wedge P\{x\}]$$

which is identical to the result of Montague's original rule  $F_2$ . Implementing Thomason's suggestion we define two new basic categories:

$$10) \quad B_{T/CN} = \left\{ \begin{array}{l} \text{every}^\circ, \text{each}^\circ, \text{the}^\circ, \text{some}^\circ, \text{a}(n)^\circ, \text{any}^\circ \\ \text{all}^*, \text{both}^*, \text{the}^*, \text{some}^*, \emptyset^*, \text{any}^* \end{array} \right\}$$

$$11) \quad B_{\overline{T}/CN} = \{ \text{all}, \text{both}, \text{the}, \text{some}, \emptyset \}$$

(where  $\emptyset$  stands for the plural of the indefinite article, ' $^\circ$ ' indicates singular, '\*' indicates distributive plural and no superscript at all (as in (11)) indicates collective plural.)

The syntactic rules that combine quantifiers with common nouns to form noun phrases are

$$12) \quad S_2(i): \quad \text{If } q \in B_{T/CN} \text{ and } \mathcal{F} \in P_{CN} \text{ then } F_1(q, \mathcal{F}) \in P_T \text{ and}$$

$$a) \quad \text{if } q = p^\circ, \text{ then } F_1(p^\circ, \mathcal{F}) = p\mathcal{F}.$$

$$b) \quad \text{if } q = p^*, \text{ then } F_1(p^*, \mathcal{F}) = p\mathcal{F}', \text{ where } \mathcal{F}' \text{ is the morphological plural of } \mathcal{F}.$$

$$S_2(ii): \quad \text{If } q \in B_{\overline{T}/CN} \text{ then } F_2(q, \mathcal{F}) \in P_{\overline{T}}, \text{ where } F_2(q, \mathcal{F}) = q\mathcal{F}' \text{ and } \mathcal{F}' \text{ is the morphological plural of } \mathcal{F}.$$

In order to account for verb agreement we shorten rule  $S_4$  in PTQ to

$$13) \quad S_4: \quad \text{If } \alpha \in P_T \text{ and } \mathcal{S} \in P_{IV} \text{ or } \alpha \in P_{\overline{T}} \text{ and } \mathcal{S} \in P_{\overline{IV}}, \text{ then } F_4(\alpha, \mathcal{S}) \in P_t, \text{ where } F_4(\alpha, \mathcal{S}) = \alpha\mathcal{S}.$$

and extend rule  $S_{17}$  to

$$14) \quad S_{17}: \quad \text{If } \Phi \in P_t, \text{ such that } \Phi = (\alpha\mathcal{S}), \text{ where } \alpha \in P_T \text{ and } \mathcal{S} \in P_{IV} \text{ or } \alpha \in P_{\overline{T}} \text{ and } \mathcal{S} \in P_{\overline{IV}}, \text{ then } F_{11}(\alpha\mathcal{S}), F_{12}(\alpha\mathcal{S}), F_{13}(\alpha\mathcal{S}), F_{14}(\alpha\mathcal{S}), F_{15}(\alpha\mathcal{S}) \text{ and } F_{16}(\alpha\mathcal{S}) \in P_t, \text{ where } F_{11}(\alpha\mathcal{S}) = \alpha\mathcal{S}' \text{ and}$$

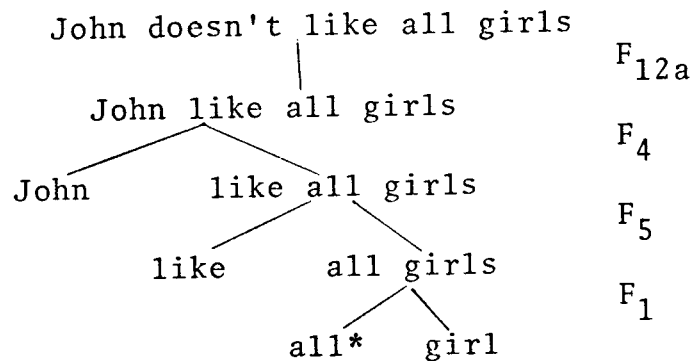
- $\delta'$  is the result of replacing the first verb in  $\delta$  by
- its third person singular present, if  $\alpha \in B_T$  or  $\alpha = F_1(p^\circ, \xi)$  (where  $\xi \in P_{CN}$ ) or  $\alpha = F_9(\beta, \gamma)$  (where  $\beta, \gamma \in P_T$ ) or  $\alpha = \{\text{he, she, it}\}$ ;
  - and otherwise by its third person plural present.

$F_{12}(\alpha \delta) = \alpha \delta''$  and  $\delta''$  is the result of replacing the first verb in  $\delta$  by

- it's negative third person singular present, if  $\alpha \in B_T$  or  $\alpha = F_1(p^\circ, \xi)$  or  $\alpha = F_9(\beta, \gamma)$  or  $\alpha = \{\text{he, she, it}\}$ ;
- and otherwise by its negative third person plural present.

According to the new rules (12), (13) and (14) the sentence

- 15) John doesn't like all girls  
can be analyzed as follows:



The translation rules corresponding to  $S_2$ ,  $S_4$ , and  $S_{17}$  are

- 16)  $T_2$ : If  $q \in B_{T/CN}$  and  $\xi \in P_{CN}$  and  $q, \xi$  translate into  $q', \xi'$ , respectively, then  $F_1(q, \xi)$  translates into  $q'(\wedge \xi')$ .

If  $q \in B_{\bar{T}/CN}$  and  $\xi \in P_{CN}$  and  $q, \xi$  translate into  $q', \xi'$ , respectively, then  $F_2(q, \xi)$  translates into  $q'(\wedge \xi')$ .

$T_4$  corresponding to rule (13) is like in PTQ.  $T_{17}$  corresponding to (14) is

- 17) If  $\phi \in P_t$ , where  $\phi$  translates as  $\phi'$ , then  $F_{11}(\phi)$  translates as  $\phi'$ ,  $F_{12}(\phi')$  translates as  $\neg \phi'$ ,

$F_{13}(\phi')$  translates as  $W(\phi')$ ,  $F_{14}(\phi')$  translates as  $\neg W(\phi')$ ,  $F_{15}(\phi')$  translates as  $H(\phi')$ ,  $F_{16}(\phi')$  translates as  $\neg H(\phi')$ .

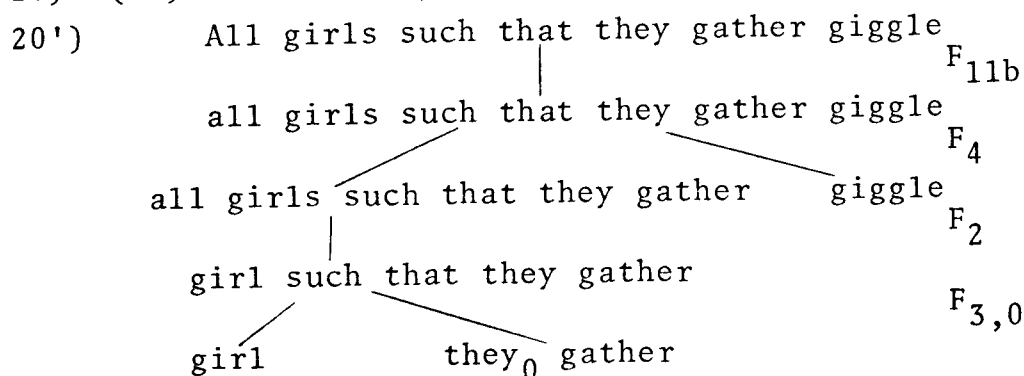
As far as the translations of the quantifiers mentioned under (10) and (11) are concerned, we will only give a tentative translation of all\* and all. (For a more comprehensive analysis of quantifiers consult R. Hausser (1974)).

18) all\*  $\in B_{\bar{T}/CN}$  translates into  $\hat{Q}\hat{P}\wedge x[\hat{Q}\{x\} \rightarrow P\{x\}]$

19) all  $\in B_{\bar{T}/CN}$  translates into  $\hat{Q}\hat{R}\wedge xR\{\hat{y}[P\{x\} \rightarrow x=y]\}$

The rules developed so far allow to translate a sentence like

20) All girls such that they gather giggle  
(where gather is of category  $\bar{IV}$  and giggle of category  $IV$ ). (20) can be analyzed as follows:



Note that they<sub>0</sub> is the collective pronoun defined in (9) above. The translation of (20') is derived as follows:

20'')  $\hat{R}\hat{R}\{\hat{y}[x_0=y]\}$  ( $\wedge$  gather')

$\hat{x}_0[\text{girl}'(x_0) \wedge \text{gather}'(\hat{y}[x_0=y])]$

$\hat{P}\wedge x[[\text{girl}'(x) \wedge \text{gather}'(\hat{y}[x=y])]] \rightarrow P x ]$

$\wedge x[[\text{girl}'(x) \wedge \text{gather}'(\hat{y}[x=y])]] \rightarrow \text{giggle}'(x)]$

Example (20) demonstrates that noun phrases of category  $T$  (i.e. all girls) can be correferential with noun phrases of category  $\bar{T}$  (i.e. they). Consider also

21) All girls such that they giggle gather  
which translates into

21'')  $\wedge x[[\text{girl}(x) \wedge \text{giggle}'(x)] \rightarrow \text{gather}'(\hat{y}[x=y])]$

(In the corresponding analysis of (21) rule  $F_2$  has to change 'he giggle' (where 'he' is a distributive pronoun to 'they giggle' - a necessary surface adjustment we omitted in (12) above).

In addition to the translation of a collective

quantifier (i.e. (19) above) we have to give the translation for collective conjunctions of noun phrases. Montague does not state the rules for a (distributive) conjunction of noun phrases, because they would involve syntactic plural (on part of the verb phrase). This restriction does not apply to the present extension. Indeed, the rules  $F_{11}$ - $F_{16}$  (see(14)) are already adjusted to handle noun phrase conjunctions in subject position. The new rule for distributive noun phrase conjunction as well as disjunction is

- 22) If  $\alpha, \beta \in P_T$ , then  $F_8(\alpha, \beta) \in P_T$  and  $F_9(\alpha, \beta) \in P_T$ ,  
 where  $F_8(\alpha, \beta) = \underline{\alpha \text{ and } \beta}$  and  $F_9(\alpha, \beta) = \underline{\alpha \text{ or } \beta}$ .

The corresponding translation rule is

- 23) If  $\alpha, \beta \in P_T$  and  $\alpha, \beta$  translate into  $\alpha', \beta'$ , respectively, then  $\underline{\alpha \text{ and } \beta}$  translates into  $\widehat{P}[\alpha'(P) \wedge \beta'(P)]$  and  $\underline{\alpha \text{ or } \beta}$  translates into  $\widehat{P}[\alpha'(P) \vee \beta'(P)]$ .

The syntactic rule for collective conjunctions of noun phrases is

- 24) If  $\alpha, \beta \in P_T$ , where  $\alpha, \beta$  are not of the form  $\underline{\text{every } \zeta}$  or  $\underline{\text{each } \zeta}$  ( $\zeta \in P_{CN}$ ), then  $F_8^*(\alpha, \beta) \in P_T$ ,  
 where  $F_8^*(\alpha, \beta) = \underline{\alpha \text{ and } \beta}$ .

The corresponding translation rule is

- 25) If  $\alpha, \beta \in P_T$  and  $\alpha, \beta$  translate into  $\alpha', \beta'$ , respectively, then  $F_8^*(\alpha, \beta) \in P_T$  and  $F_8^*(\alpha, \beta)$  translates into  $\widehat{R}[R\{\widehat{x} \alpha'(\widehat{z}[x=z]) \vee \beta'(\widehat{z}[x=z])\}]$ .

Note that the input to (24) and (25) are distributive noun phrases, i.e. noun phrases of category T.

According to (25) the sentence

- 26) A boy and a girl collided  
 (where collide  $\in P_{IV}$ ) translates as

$\widehat{R}[R\{\widehat{x} \widehat{P}V_y[\text{boy}'(y) \wedge P\{y\}](\widehat{z}[z=x]) \vee \widehat{P}V_w[\text{girl}'(w) \wedge P\{w\}](\widehat{z}[x=z])\}]$  (^ collide')

which reduces to

collide'  $\{\widehat{x} V_y[\text{boy}'(y) \wedge y=x] \vee V_w[\text{girl}'(w) \wedge w=x]\}$

Also sentences like

- 27) John mixed the bulbs and planted them  
 where mix is an IV/ $\overline{T}$ -phrase and plant is an IV/T-phrase won't pose any problem in our extension once we provide the (straightforward) adjustments in  $S_5(T_5)$  and  $S_{14}(T_{14})$ .

- 28) If  $\delta \in P_{IV/T}$  and  $\beta \in P_T$  or  $\delta \in P_{IV/\bar{T}}$  and  $\beta \in P_{\bar{T}}$ , then  $F_5(\delta, \beta) \in P_{IV}$ , where  $F_5(\delta, \beta) = \delta\beta$  if  $\beta$  does not have the form  $\left\{ \begin{matrix} \text{he}_n \\ \text{they}_n \end{matrix} \right\}$  and  $F_5(\delta, \left\{ \begin{matrix} \text{he}_n \\ \text{they}_n \end{matrix} \right\}) = \delta \left\{ \begin{matrix} \text{him} \\ \text{them} \end{matrix} \right\}$

The corresponding translation rule is

- 29) If  $\delta \in P_{IV/T}$  and  $\beta \in P_T$  or  $\delta \in P_{IV/\bar{T}}$  and  $\beta \in P_{\bar{T}}$ , and  $\delta, \beta$  translate into  $\delta', \beta'$ , respectively, then  $F_5(\delta, \beta)$  translates into  $\delta'(\wedge \beta')$ .

$S_{14}$  in PTQ is replaced by

- 30) If  $\alpha \in P_T$  and  $\phi \in P_t$ , then  $F_{10,n}(\alpha, \phi) \in P_t$ , where either
- (i)  $\alpha \in B_T$  or  $\alpha$  has the form  $F_1(p^\circ, \wp)$  - where  $\wp \in P_{CN}$  - or  $\alpha = F_9(\beta, \gamma)$  - where  $\beta, \gamma \in P_T$  - and  $F_{10,n}$  comes from  $\phi$  by replacing the first occurrence of  $\underline{\text{he}}_n$  or  $\underline{\text{him}}_n$  by  $\alpha$  and all other occurrences of  $\underline{\text{he}}_n$  or  $\underline{\text{him}}_n$  by  $\{\text{he, she, it}\}$  or  $\{\text{her, she, it}\}$ , respectively, according as the gender of the first  $B_{CN}$  or  $B_T$  in  $\alpha$  is  $\{\text{masc., fem., or neuter}\}$ ;
- (ii)  $\alpha$  has the form  $F_1(p^*, \wp)$  or  $F_2(p, \wp)$  - where  $p^* \in B_{T/CN}$ ,  $p \in B_{\bar{T}/CN}$  and  $\wp \in P_{CN}$ , and  $F_{10,n}$  comes from  $\phi$  by replacing the first occurrence of  $\underline{\text{he}}_n$ ,  $\underline{\text{him}}_n$ ,  $\underline{\text{they}}_n$ , or  $\underline{\text{them}}_n$  by  $\alpha$  and all other occurrences of  $\underline{\text{he}}_n$ ,  $\underline{\text{him}}_n$ ,  $\underline{\text{they}}_n$  or  $\underline{\text{them}}_n$  by  $\underline{\text{they}}$  or  $\underline{\text{them}}$ , respectively.
- (iii)  $\alpha = \text{he}_k$  and  $F_{10,n}(\alpha, \phi)$  comes from  $\phi$  by replacing all occurrences of  $\underline{\text{he}}_k$ ,  $\underline{\text{him}}_k$ ,  $\underline{\text{they}}_k$  or  $\underline{\text{them}}_k$  by  $\underline{\text{he}}_n$ ,  $\underline{\text{him}}_n$ ,  $\underline{\text{they}}_n$ , or  $\underline{\text{them}}_n$ , respectively.

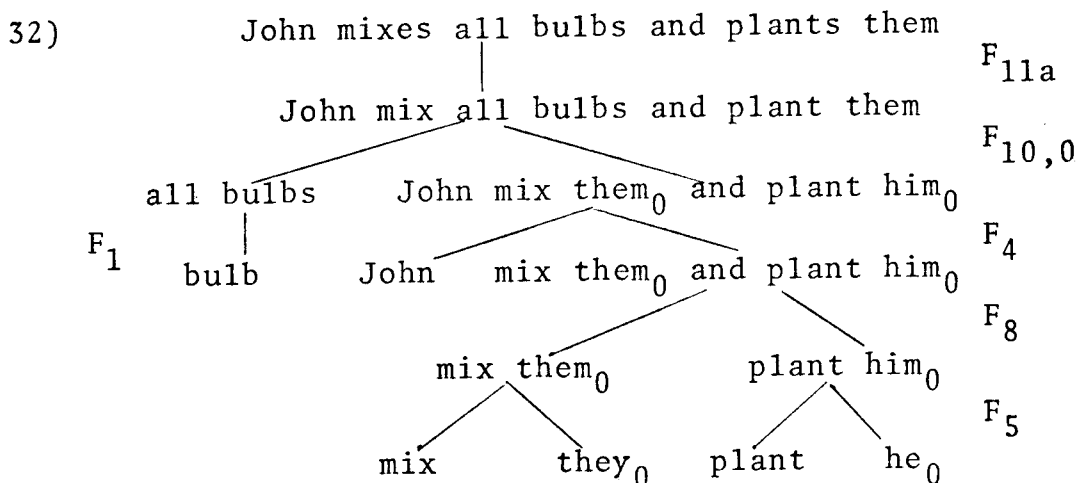
The corresponding translation rule (i.e.  $T_{14}$  in PTQ) is changed to

- 31) If  $\alpha \in P_T$ ,  $\phi \in P_t$ , and  $\alpha, \phi$  translate into  $\alpha', \phi'$ , respectively, then  $F_{10,n}(\alpha, \phi)$  translates into  $\alpha'(x_n \phi')$  or  $\alpha'(P_n \phi')$  depending on whether the first variable in  $\phi$  is  $\underline{\text{he}}_n$  ( $\underline{\text{him}}_n$ ) or  $\underline{\text{they}}_n$  ( $\underline{\text{them}}_n$ ).

Note that our new rules of quantification (i.e. (30) and (31)) introduce only noun phrases of category T, but not of category  $\bar{T}$ . The mechanism of this approach



can be seen in the translation of sentences (27), which is analyzed as:



The translation of (32) is derived as follows:

32'')  $\hat{P}P\{\hat{\wedge}j\}(\hat{z}[\text{mix}'(\hat{R}R\{\hat{y}[y=x_0]\})(z) \wedge \text{plant}'(\hat{P}P\{x_0\})(z)])$   
 which reduces to  
 $\text{mix}'(\hat{\wedge}j, \hat{R}R\{\hat{y}[y=x_0]\}) \wedge \text{plant}'(\hat{\wedge}j, \hat{P}P\{x_0\})$

rule of quantification:

$\hat{P}\wedge x[\text{bulb}'(x) \rightarrow P\{x\}](\hat{\wedge}j, \hat{R}R\{\hat{y}[y=x_0]\}) \wedge \text{plant}'(\hat{\wedge}j, \hat{P}P\{x_0\})$   
 $\wedge x[\text{bulb}'(x) \rightarrow \text{mix}'(\hat{\wedge}j, \hat{R}R\{\hat{y}[y=x]\}) \wedge \text{plant}'(\hat{\wedge}j, \hat{P}P\{x\})]$

Thus the translation of all bulbs binds the ' $x_0$ ' occurring in the translation of they<sub>0</sub> as well as of he<sub>0</sub>.

33) In order to derive sentences like  
 all boys (each) played the piano and (then)  
 lifted it (together).

we have to make a little adjustment in the rules for the conjunction of verbphrases, i.e. S<sub>12</sub> and T<sub>12</sub> in PTQ. The reason is that in (33) we conjoin an IV-phrase (play) and an IV-phrase (lift). S<sub>12</sub> in PTQ is replaced by

34) If  $\gamma, \delta \in P_{IV}$  or  $P_{IV}$ , then  $F_8(\gamma, \delta), F_9(\gamma, \delta) \in P_{IV}$ .

The translation rule T<sub>12</sub> in PTQ is replaced by

35) If  $\gamma \in P_{IV}$  and  $\delta \in P_{IV}$  and  $\gamma, \delta$  translate into  $\gamma', \delta'$  respectively, then  $\gamma$  and  $\delta$  translates into  $\hat{x}[\gamma'(\hat{y}[x=y]) \wedge \delta'(x)]$ .

If  $\gamma \in P_{IV}$  and  $\delta \in P_{IV}$ , then  $\gamma$  and  $\delta$  translates into  $\hat{x}[\gamma'(x) \wedge \delta'(\hat{y}[y=x])]$ .

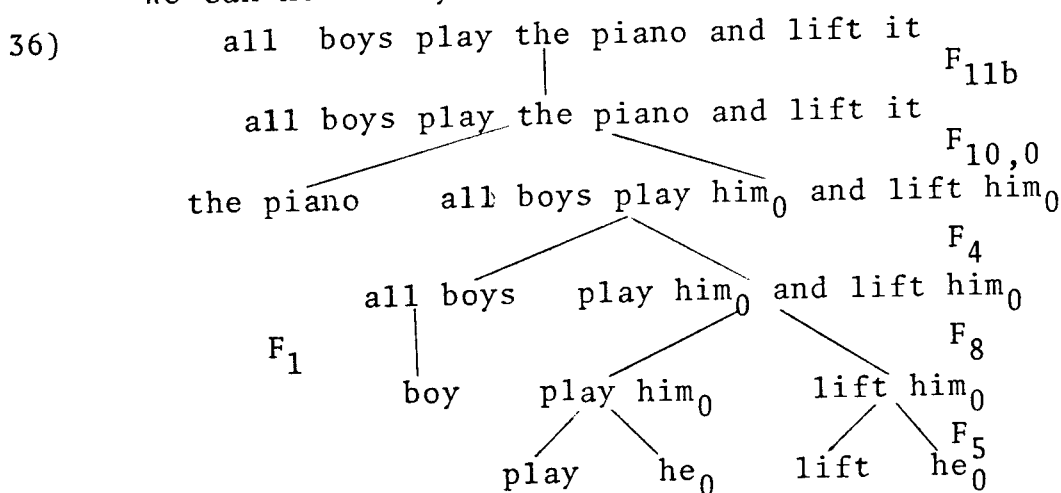
If  $\gamma \in P_{IV}$  and  $\delta \in P_{IV}$ , then  $\underline{\gamma}$  and  $\underline{\delta}$  translate into  $\hat{x}[\gamma'(x) \wedge \delta'(x)]$ .

If  $\gamma \in P_{IV}$  and  $\delta \in P_{IV}$ , then  $\underline{\gamma}$  and  $\underline{\delta}$  translate into  $\hat{x}[\gamma'(\hat{y}[y=x]) \wedge \delta'(\hat{z}[z=x])]$

and similarly for or.

Note that the output of (34) are simply IV-phrases (and not  $\overline{IV}$ -phrases - no matter what kind of verbs were conjoined). Thus the output of (34) combines simply with a distributive noun phrase to form a sentence.

We can now analyze sentence (33) as follows:



The translation of (36) runs as follows:

36'')  $\text{play}'(\hat{PP}\{x_0\})$  ;  $\text{lift}'(\hat{PP}\{x_0\})$

The new rule  $T_{12}$  (see 35 above) generates

$\hat{y}[\text{play}'(\hat{PP}\{x_0\})(\hat{z}[z=y]) \wedge \text{lift}'(\hat{PP}\{x_0\})(y)]$

$T_4$  results in

$\wedge x[\text{boy}'(x) \rightarrow [\text{play}'(\hat{z}[z=x], \hat{PP}\{x_0\}) \wedge \text{lift}'(x, \hat{PP}\{x_0\})]]$

Finally, application of  $T_{14}$  (see 31 above) gives:

$\forall y[\wedge w[\text{piano}'(w) \leftrightarrow w=y] \wedge \wedge x[\text{boy}'(x) \rightarrow [\text{play}'(\hat{z}[z=x], \hat{PP}\{y\}) \wedge \text{lift}'(x, \hat{PP}\{y\})]]]$ .

In order to implement plural into PTQ we defined the following new sets of basic expressions:

$B_{T/CN} = \{\text{every}^\circ, \text{each}^\circ, \text{the}^\circ, \text{some}^\circ, \text{a(n)}^\circ, \text{any}^\circ, \text{all}^*, \text{both}^*, \text{the}^*, \text{some}^*, \emptyset^*, \text{any}^*\}$

$B_{T/CN} = \{\text{all}, \text{both}, \text{the}, \text{some}, \emptyset\}$

$$\begin{aligned}
B_{\bar{T}} &= \{ \text{they}_n \} \\
B_{\bar{IV}/T} &= \{ \text{mix, correlate, adress, ...} \} \\
B_{IV/\bar{T}} &= \{ \text{lift, prepare, form, ...} \} \\
B_{\bar{IV}} &= \{ \text{gather, collide, be numerous, marry, be} \\
&\quad \{ \text{similar, ...} \}
\end{aligned}$$

Furthermore, we replaced  $S_2$  (in PTQ) by (12),  $T_2$  by (16),  $S_4$  by (13),  $S_5$  by (28),  $T_5$  by (29),  $S_{12}$  by (34),  $T_{12}$  by (35),  $S_{13}$  by (22) and (24),  $T_{13}$  by (23) and (25),  $S_{17}$  by (14) and  $T_{17}$  by (17).

By making number a feature of the quantifier rather than the noun we arrived at a straightforward and formally explicit extension of PTQ, that handles coreference between collective and distributive plural noun phrases.

#### Footnote:

1) The reason is that the formation of restrictive relative clauses in PTQ cannot handle sentences like  
John watered some of the tulips and all of the roses that bloomed.

(on the reading, where the relative clause modifies both, tulips and roses.)

Thus it is necessary to provide a new treatment for both, the formation of restrictive relative clauses (for arbitrary long conjunctions of headnouns) and the independent quantification of multiple headnouns. It is this latter rule that would account for the surface adjustment (he giggle  $\rightarrow$  they giggle) in (21).

For a complete treatment of restrictive relative clauses with multiple headnouns see R. Hausser (1974).

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